

65. In the radioactive decay of Eq. 21-13, a ^{238}U nucleus transforms to ^{234}Th and an ejected ^4He . (These are nuclei, not atoms, and thus electrons are not involved.) When the separation between ^{234}Th and ^4He is $9.0 \times 10^{-15} \text{ m}$, what are the magnitudes of (a) the electrostatic force between them and (b) the acceleration of the ^4He particle?

The radioactive decay mentioned is
 $^{238}\text{U} \rightarrow ^{234}\text{Th} + ^4\text{He}$.

^{234}Th has 90 protons and ^4He has 2.

Charge of a proton is $e = 1.602 \times 10^{-19}$.

The electrostatic force between Th and He is thus the electrostatic force between 90 protons and 2 protons.

$$F = k \frac{q_1 q_2}{r^2} = (8.99 \times 10^9) \frac{(90 \times 1.602 \times 10^{-19})(2 \times 1.602 \times 10^{-19})}{(9.0 \times 10^{-15})^2} = 5.1 \times 10^2 \text{ N}$$

Proton mass $m_p = 1.67 \times 10^{-27} \text{ kg}$.

Neutron mass $m_n = 1.68 \times 10^{-27} \text{ kg}$.

^4He has 2 protons and 2 neutrons (we don't take into consideration the electrons as the question tells us that no electrons are involved).

Thus, mass of ^4He particle is

$$m_{\text{He}} = 2m_p + 2m_n = 2 \times 1.67 \times 10^{-27} + 2 \times 1.68 \times 10^{-27} = 6.70 \times 10^{-27} \text{ kg}$$

$$a_{\text{He}} = \frac{F}{m_{\text{He}}} = \frac{5.1 \times 10^2 \text{ N}}{6.70 \times 10^{-27} \text{ kg}} = 7.7 \times 10^{28} \frac{\text{m}}{\text{s}^2}$$